DATA-140.


Probability for Data Science

## WEEK 3 STUDY GUIDE

## The Big Picture

The week starts with another connection between the binomial and Poisson families, and moves on to the most important concept of the course, which is expectation. This can be thought of as a kind of center of the distribution of a random variable, or a good guess for the variable. All probabilities are expectations, the variance of a random variable is an expectation, and least squares predictors are expectations. So please pay attention!

- Randomizing parameters can have dramatic effects on dependence and independence. A Poisson number of i.i.d. success/failure trials has beautiful and powerful properties.
- Expectation is the average of the possible values, weighted by their probabilities. Care is needed for variables that have infinitely many values.
- The definition helps us calculate some expectations, but almost always we calculate expectation using its properties, just as we calculate derivatives using properties of derivatives instead of the definition.
- A simple but powerful method helps us find the expectation of a function of a random variable.


## Week At a Glance

| Mon 1/29 | Tue 1/30 | Wed 1/31 | Thu 2/1 | Fri 2/2 |
| :--- | :--- | :--- | :--- | :--- |
|  | Lecture | Sections | Lecture | Mega Sections |
| Lab 2 due <br> Lab 3A (Due Mon 2/5) |  |  | Lab 3A Party 9-11 |  |
| HW 2 Due |  |  |  |  |
| HW 3 (Due Mon 2/5) |  |  |  | HW 3 Party 2pm - |
| Skim 7.1, 7.2 | Work through Ch 7 | Finish Ch 7, skim 8.1 | Work through 8.1-8.2 | Finish 8.1-8.3 |

## Reading, Practice, and Class Meetings

| Book | Topic | Lectures: Prof. A. | Sections: TAs | Optional Additional Practice |
| :---: | :---: | :---: | :---: | :---: |
| Ch 7 | Poissonization <br> - 7.1 has properties of the Poisson distribution -7.2 asks the same questions as 6.1, but with a Poisson number of trials -7.3 extends this to trials with more than two categories, analogous to 6.3 | Tue 1/31 <br> Poissonization: <br> - Beautiful calculations with surprising results <br> - Pay attention to the math because you'll need the methods again | Wed 2/1 <br> - Ch 7 Ex 2, 7, 8 | Chapter 7 <br> All the exercises |
| Ch 8 | Expectation <br> - 8.1 has the definition, interpretation, and a note on existence <br> - 8.2 calculates the expectations of some of the famous distributions, in one case by introducing a new way of calculating expectation -8.3 shows how to calculate expectations of linear and nonlinear functions of random variables | Thu 2/2 <br> - Focused on 8.1-8.3 <br> - Fine points, nonlinear functions, and some surprises | Fri 2/3 <br> -Ch 8 Ex 2, 10, 6, 4 | Chapter 8 <br> Wait till next week; you need the remaining sections of Ch 8 for the remaining exercises in the chapter |

