

## Spring 2024 WEEK 9 STUDY GUIDE

## **The Big Picture**

More technique! And establishing some normal distribution results we have taken for granted without proof.

- To study the joint behavior of two random variables, we define their joint density, which is the analog of the discrete joint distribution. Probabilities and expectations are now double integrals.
- The family of beta densities is important for machine learning and offers a good example of how joint densities can be constructed.
- We establish some basic properties of the standard normal. We notice connections with gamma distributions. By simulation, we
  notice key properties of sums: sums of independent normals are normal, and sums of independent gammas (with the same rate)
  are gamma.
- The two most important branches of the gamma family have integer or half-integer shape parameters.

## **Week At a Glance**

Mon 3/11	Tue 3/12	Wed 3/13	Thu 3/14	Fri 3/15
	Lecture	Sections	Lecture	Mega Sections
Lab 6A Due Lab 6B (Due NOON Mon 3/18)			Lab 6B Party 10 AM to noon	
HW 8 Due HW 9 (Due NOON Mon 3/18)				HW 9 Party 2 PM to 5 PM
Skim Sec 17.1	Work through Sec 17.1 carefully, skim Sections 17.2-3	Work through Chapter 17	Work through Chapter 17	Review for midterm

## **Reading, Practice, and Class Meetings**

Book	Topic	Lectures: Prof. A.	Sections: TAs	Optional Additional Practice
Ch 17	Joint Densities - 17.1-17.3 are the 2-dimensional counterparts of Ch 15 and the density version of Chapter 4. The examples in the videos aren't always the same as those in the text 17.4 is one of the "big name" families of densities	Tuesday 3/12 - Joint densities - The beta family	Wednesday 3/13 - Ch 17 Ex 2, 4, 7	Ch 17 - Ex 1, 9
Ch 18	Normal and gamma families  - 18.1 establishes the normal density, mean, and variance, and in the process discovers an important fact about sums of squares of standard normals. You have to know the results even if you don't follow some of the proofs.  - 18.2 observes by simulation that sums of independent normals are normal, and uses this in exercises  - 18.3 observes by simulation that sums of independent gammas with the same rate are gamma, and studies one major branch of the gamma family  - 18.4 studies the other major branch	Thursday 3/14  - Fundamental properties of the standard normal - The gamma family and its relation to squares of centered normals	Friday 3/15 - Past midterm questions	Postponed till next week. Study for the midterm.